

Revisiting the annihilation decay $\bar{B}_s \rightarrow \pi^+ \pi^-$

Yadong Yang^a, Fang Su, Gongru Lu, Hongjun Hao

Department of Physics, Henan Normal University, Xinxiang, Henan 453007, P.R. China

Received: 5 May 2005 /

Published online: 13 September 2005 – © Springer-Verlag / Società Italiana di Fisica 2005

Abstract. It is very important to know the strength of the annihilation contribution in B charmless non-leptonic decays. The $\bar{B}_s \rightarrow \pi^+ \pi^-$ process could serve as a good probe of the strength. We have studied the process in the QCD factorization framework. Using a gluon mass scale dictated by the studies of infrared behavior of gluon propagators to avoid enhancements in the soft endpoint regions, we find that the CP averaged branching ratio is about 1.24×10^{-7} , the direct CP asymmetry $C_{\pi\pi}$ is about -0.05 , while the mixing-induced CP asymmetry is quite large with the value $S_{\pi\pi} = 0.18$. This process could be measured at LHC-b experiments in the near future and would deepen our understanding of the dynamics of B charmless decays.

PACS. 13.25.Hw, 12.38.Bx, 12.38.Aw

1 Introduction

In recent years many efforts have been made to understand charmless decays of B mesons, which provide good grounds to get deep insights into the flavor structure of the standard model (SM), the origin of CP violation, the dynamics of hadronic decays, and to search for any signals of new physics beyond the SM. Up to now, BaBar (SLAC) [1] and Belle (KEK) [2] have already accumulated a large set of data and have made plenty of exciting measurements. Moreover, in the near future LHC-b experiment, the expected number of $b\bar{b}$ events produced per year is about 10^{12} , and it is noted that 10% of the events would fragment to B_s mesons. This high statistics will allow for studies of rare B_s decay modes, which will provide very sensitive tests of theories for B decays, electro-weak interaction models and so on.

For non-leptonic B meson decays, the most difficult aspect lies in the computation of the matrix elements of the effective four-quark operators between hadron states. To deal with this, a simple and widely used approach is the so-called factorization approach (FA) [3]. In the past few years, new approaches, such as the QCD factorization (QCDF) [4] and the perturbation QCD (pQCD) scheme [5] have been proposed to improve the FA on QCD grounds.

In most cases of the B meson non-leptonic decays, the annihilation contribution carries weak and strong phases different from that provided by the tree or penguin amplitudes, which is very important for studying CP violating observables. Meanwhile, the calculation of annihilation contributions is interesting by itself, since it can help us to understand the low energy QCD dynamics and the viability of the theoretical approaches. As argued in [4],

the annihilation amplitude is formally power suppressed by the order Λ_{QCD}/m_b in QCDF. However, the annihilation contribution may not be small. In a recent systematic calculation of B decays [6], it is shown that the annihilation contributions could cause considerable uncertainties in their theoretical predictions, where the contributions are parameterized in terms of the divergent integral $\int_0^1 \frac{dy}{y} \rightarrow X_A = (1 + \varrho_A e^{i\varphi}) \ln \frac{m_B}{\Lambda_b}$. In this paper, we argue that the strength of the annihilation could be probed by measuring the interesting decay mode $\bar{B}_s \rightarrow \pi^+ \pi^-$, which is a pure annihilation process. In our calculation of the scattering kernel, we will use the Cornwall [7] prescription of the gluon propagator with a dynamical mass to avoid enhancements in the soft endpoint. It is very interesting to note that recent theoretical [8] and phenomenological [9] studies are now accumulating that support a softer infrared behavior for gluon propagator. Besides serving as a probe for the annihilation, the decay has some interesting features: sizable CP violation due to both tree and penguin operators contributing, and clear experimental signatures due to its two charge final states. Moreover, if a few percents of the final pions are mis-identified to be muons, it would bring considerable uncertainties to the measurement of $\bar{B}_s \rightarrow \mu^+ \mu^-$ at LHC-b. Therefore, the decay deserves our theoretical studies using different approaches.

We have found that the CP averaged branching ratio of the $\bar{B}_s \rightarrow \pi^+ \pi^-$ decay is about 1.24×10^{-7} , the direct CP asymmetry $C_{\pi\pi}$ is about -0.05 , while the mixing-induced CP asymmetry is as large as $S_{\pi\pi} = 0.18$. Our results might be tested in the near future at LHC-b.

The remaining parts of this paper are organized as follows. In the next section, we outline the necessary ingredients of the QCD factorization approach for describing

^a Corresponding author: e-mail: yangyd@henannu.edu.cn

the $\bar{B}_s \rightarrow \pi^+\pi^-$ decay and calculate the decay amplitude. In Sect. 3, we give the numerical results of the CP averaged branching ratio and discuss the CP asymmetries in the $\bar{B}_s \rightarrow \pi^+\pi^-$ decay.

2 $\bar{B}_s \rightarrow \pi^+\pi^-$ decay in the QCD factorization approach

We will start as usual from the effective Hamiltonian for the $\Delta B = 1$ transitions given by [10]

$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} \left\{ V_{ub}V_{us}^* [C_1(\mu)O_1(\mu) + C_2(\mu)O_2(\mu)] - V_{tb}V_{ts}^* \sum_{i=3}^{10} C_i(\mu)O_i(\mu) \right\} + \text{h.c.}, \quad (1)$$

where C_i are the Wilson coefficients at the renormalization scale μ in the standard model by integrating out heavy gauge bosons and top quark fields. $O_{1,2}$ are tree operations arising from W -boson exchange, and O_{3-10} are penguin operators. The values for C_i and the definition of the operators O_i could be found in [10].

With the effective Hamiltonian, the amplitude for $\bar{B}_s \rightarrow \pi^+\pi^-$ in a naive factorization is

$$\begin{aligned} \mathcal{A}(\bar{B}_s \rightarrow \pi^+\pi^-) &= -2 \frac{G_F}{\sqrt{2}} V_{tb}V_{ts}^* \\ &\times \left[\left(a_3 + \frac{3}{2} Q_u a_9 \right) \langle \pi^+\pi^- | \bar{u}\gamma_\mu L u | 0 \rangle \langle 0 | \bar{s}\gamma^\mu R b | \bar{B}_s \rangle \right. \\ &\quad \left. + \left(a_5 + \frac{3}{2} Q_u a_7 \right) \langle \pi^+\pi^- | \bar{u}\gamma_\mu R u | 0 \rangle \langle 0 | \bar{s}\gamma^\mu L b | \bar{B}_s \rangle \right] \\ &+ \frac{G_F}{\sqrt{2}} V_{ub}V_{us}^* a_2 \langle \pi^+\pi^- | \bar{u}\gamma_\mu L u | 0 \rangle \langle 0 | \bar{s}\gamma^\mu L b | \bar{B}_s \rangle \\ &+ (u \rightarrow d) \\ &= -2i \frac{G_F}{\sqrt{2}} V_{tb}V_{ts}^* f_{B_s} p_B^\mu \left[\left(a_3 + \frac{3}{2} Q_u a_9 \right) \langle \pi^+\pi^- | \bar{u}\gamma_\mu L u | 0 \rangle \right. \\ &\quad \left. + \left(a_5 + \frac{3}{2} Q_u a_7 \right) \langle \pi^+\pi^- | \bar{u}\gamma_\mu R u | 0 \rangle \right] \\ &+ i \frac{G_F}{\sqrt{2}} V_{ub}V_{us}^* f_{B_s} p_B^\mu a_2 \langle \pi^+\pi^- | \bar{u}\gamma_\mu L u | 0 \rangle + (u \rightarrow d), \end{aligned} \quad (2)$$

where $L, R = (1 \mp \gamma_5)/2$. Due to the conservation of the vector current and partial conservation of the axial-vector current, this amplitude will vanish in the limit $m_u, m_d \rightarrow 0$. To α_s order, the matrix $\langle \pi^+\pi^- | u \not{P}_B (1 - \gamma_5) u | 0 \rangle$ also vanishes due to the cancellation between the amplitudes of Fig. 1a,b, so that the non-factorizable contribution will dominate the decay, which can be obtained by calculating the amplitudes of Fig. 1c,d. We consider the contribution up to the twist-3 distribution amplitude of the light mesons

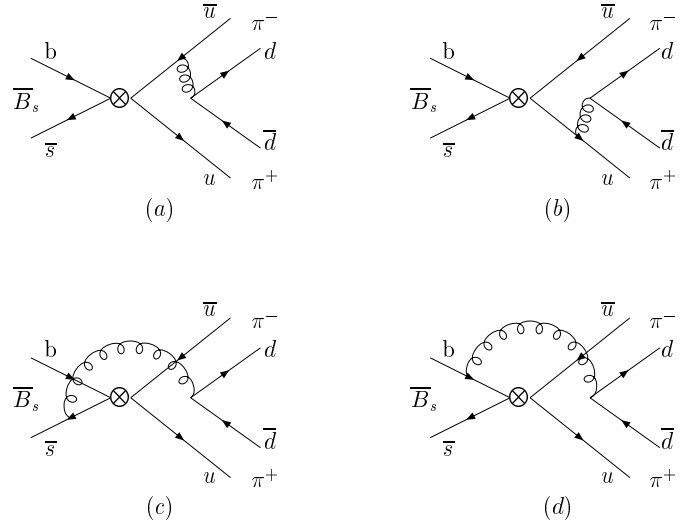


Fig. 1a–d. The annihilation diagrams for $\bar{B}_s \rightarrow \pi^+\pi^-$ decay

which is superficially suppressed by μ_π , however, μ_π is much larger than its naive scaling estimate Λ_{QCD} [4]:

$$\mu_\pi = \frac{m_\pi^2}{m_u + m_d} = 1.5 \text{ GeV}. \quad (3)$$

The amplitudes are calculated to be

$$\begin{aligned} \mathcal{A}^T(\bar{B}_s \rightarrow \pi^+\pi^-) &= \frac{G_F}{\sqrt{2}} f_{B_s} f_\pi^2 \pi \alpha_s(\mu) \frac{C_F}{N_C^2} C_1 \\ &\times \int_0^\infty dl_+ \int_0^1 dx \int_0^1 dy \left\{ \Phi_\pi(x) \Phi_\pi(y) \right. \\ &\quad \times \left[(x\Phi_+^B(l_+) + \xi\Phi_-^B(l_+)) \frac{M_B^4}{D_s k_g^2} \right. \\ &\quad \left. \left. + (\xi - y)\Phi_-^B(l_+) \frac{M_B^4}{D_b k_g^2} \right] \right. \\ &\quad \left. + \frac{\mu_\pi^2}{m_B^2} \phi_\pi(x) \phi_\pi(y) \right. \\ &\quad \times \left[(x\Phi_+^B(l_+) + y\Phi_-^B(l_+) + 3\xi\Phi_-^B(l_+)) \frac{M_B^4}{D_s k_g^2} \right. \\ &\quad \left. + \left(\bar{x}\Phi_+^B(l_+) + \bar{y}\Phi_-^B(l_+) + 3\xi\Phi_-^B(l_+) \right. \right. \\ &\quad \left. \left. - 2 \frac{m_b}{m_B} (\Phi_+^B(l_+) + \Phi_-^B(l_+)) \right) \right] \frac{M_B^4}{D_b k_g^2} \left. \right\}, \end{aligned} \quad (4)$$

$$\begin{aligned} \mathcal{A}^P(\bar{B}_s \rightarrow \pi^+\pi^-) &= \frac{G_F}{\sqrt{2}} f_{B_s} f_\pi^2 \pi \alpha_s(\mu) \frac{C_F}{N_C^2} \\ &\times \int_0^\infty dl_+ \int_0^1 dx \int_0^1 dy \end{aligned}$$

$$\begin{aligned}
& \times \left\{ \Phi_\pi(x)\Phi_\pi(y) \left[\left(2C_4 + \frac{C_{10}}{2} \right) \right. \right. \\
& \quad \times \left((x\Phi_+^B(l_+) + \xi\Phi_-^B(l_+)) \frac{M_B^4}{D_s k_g^2} \right. \\
& \quad \quad \left. \left. + (\xi - y)\Phi_-^B(l_+) \frac{M_B^4}{D_b k_g^2} \right) \right. \\
& \quad \left. + \left(2C_6 + \frac{C_8}{2} \right) \left((\xi_B - x)\Phi_+^B(l_+) + \xi\Phi_-^B(l_+) \frac{M_B^4}{D_b k_g^2} \right. \right. \\
& \quad \quad \left. \left. + y\Phi_-^B(l_+) \frac{M_B^4}{D_s k_g^2} \right) \right] \\
& + \left(2C_4 + 2C_6 + \frac{C_8}{2} + \frac{C_{10}}{2} \right) \frac{\mu_\pi^2}{m_B^2} \phi_\pi(x)\phi_\pi(y) \\
& \times \left[(\bar{x}\Phi_+^B(l_+) + \bar{y}\Phi_-^B(l_+) + 3\xi\Phi_-^B(l_+)) \right. \\
& \quad \left. - 2\frac{m_b}{m_B} (\Phi_+^B(l_+) + \Phi_-^B(l_+)) \frac{M_B^4}{D_b k_g^2} \right. \\
& \quad \left. + (x\Phi_+^B(l_+) + y\Phi_-^B(l_+) + 3\xi\Phi_-^B(l_+)) \frac{M_B^4}{D_s k_g^2} \right] \Big\}, \quad (5)
\end{aligned}$$

where $\bar{x} = 1 - x$, $\xi_B = (M_B - m_b)/M_B$, and $\xi = l_+/M_B$. $D_{b,s}$ and k_g^2 are the virtualities of b quark, s quark and gluon propagators respectively. The Φ are the leading twist light-cone distribution amplitudes (DA) of π and B mesons. $\phi_\pi(x)$ is the twist-3 DA of the π meson. These distribution amplitudes can be found in [11–14] which describe the long-distance QCD dynamics of the matrix elements of quarks and mesons, which are factorized out from the perturbative short-distance interactions in the hard scattering kernels. For the distribution functions of the B meson, we use the model proposed in [11]:

$$\Phi_+^B(l_+) = \sqrt{\frac{2}{\pi\lambda^2}} \frac{l_+^2}{\lambda^2} \exp\left[-\frac{l_+^2}{2\lambda^2}\right], \quad (6)$$

$$\Phi_-^B(l_+) = \sqrt{\frac{2}{\pi\lambda^2}} \exp\left[-\frac{l_+^2}{2\lambda^2}\right]. \quad (7)$$

Now we can write the total decay amplitude

$$\begin{aligned}
\mathcal{A}(\bar{B}_s \rightarrow \pi^+\pi^-) & \quad (8) \\
& = V_{ub}V_{us}^*\mathcal{A}^T - V_{tb}V_{ts}^*\mathcal{A}^P = V_{ub}V_{us}^*\mathcal{A}^T[1 + ze^{i(\gamma+\delta)}],
\end{aligned}$$

where

$$z = |V_{tb}V_{ts}^*/V_{ub}V_{us}^*| |\mathcal{A}^P/\mathcal{A}^T|, \quad \gamma = \arg[V_{tb}V_{ts}^*/V_{ub}V_{us}^*],$$

and δ is the relative strong phase between penguin and tree contribution amplitudes, and z and δ can be calculated within the QCD factorization framework.

3 Numerical results and summary

We list the parameters used in our numerical calculation [15]:

$$M_{B_s} = 5.37 \text{ GeV}, \quad m_b = 4.66 \text{ GeV}, \quad \tau_{B_s^0} = 1.461 \text{ ps}, \quad (9)$$

$$f_{B_s} = 236 \text{ MeV}, \quad f_\pi = 130 \text{ MeV}, \quad \bar{\rho} = 0.20, \quad \bar{\eta} = 0.33.$$

We set the scale in $\alpha_s(\mu)$ to be $M_{B_s}/2$ which is about the averaged virtuality of the time-like gluon. In (4) and (5) we meet with endpoint divergences, which is the known difficulty in dealing with the annihilation diagram within the QCD factorization framework. Instead of the widely used treatment $\int_0^1 \frac{dy}{y} \rightarrow X_A = (1 + \varrho_A e^{i\varphi}) \ln \frac{m_B}{\Lambda_h}$ in the literature [16–18], we use an effective gluon propagator [7] to avoid enhancements in the soft endpoint region:

$$\begin{aligned}
\frac{1}{k^2} & \Rightarrow \frac{1}{k^2 + M_g^2(k^2)}, \\
M_g^2(k^2) & = m_g^2 \left[\frac{\ln\left(\frac{k^2 + 4m_g^2}{\Lambda^2}\right)}{\ln\left(\frac{4m_g^2}{\Lambda^2}\right)} \right]^{-\frac{12}{11}}. \quad (10)
\end{aligned}$$

Typically $m_g = 500 \pm 200 \text{ MeV}$, $\Lambda = \Lambda_{\text{QCD}} = 250 \text{ MeV}$. The use of this gluon propagator is supported by lattice results [19] and field theoretical studies [8, 20] which have shown that the gluon propagator is not divergent as fast as $\frac{1}{k^2}$.

For the twist-3 DA $\phi_\pi(x)$, its asymptotic form is $\phi_\pi(x) = 1$ [13] which is used in [6, 18]. To further suppress endpoint contributions, we will use the recent model by Huang and Wu [14]:

$$\begin{aligned}
\phi_\pi(x) & \quad (11) \\
& = \frac{A_p \beta^2}{2\pi^2} \left[1 + B_p C_2^{1/2} (1 - 2x) + C_p C_4^{1/2} (1 - 2x) \right] \\
& \quad \times \exp\left[-\frac{m^2}{8\beta^2 x(1-x)}\right],
\end{aligned}$$

where $C_2^{1/2}(1 - 2x)$ and $C_4^{1/2}(1 - 2x)$ are the Gegenbauer polynomials and the other parameters could be found in [14].

Using these inputs, we get the CP averaged branching ratio of the decay:

$$\text{Br}(\bar{B}_s \rightarrow \pi^+\pi^-) = (1.24 \pm 0.28) \times 10^{-7}. \quad (12)$$

The available upper limit of the decay at 90% confidence level [15] is

$$\text{Br}(\bar{B}_s \rightarrow \pi^+\pi^-) < 1.7 \times 10^{-4}. \quad (13)$$

Obviously, our result is far below this upper limit. However, our result is larger than these QCD factorization results, $\text{Br}(\bar{B}_s \rightarrow \pi^+\pi^-) \simeq 2 \times 10^{-8}$ [6, 18], by using the treatment $\int_0^1 \frac{dy}{y} \rightarrow X_A = (1 + \varrho_A e^{i\varphi}) \ln \frac{m_B}{\Lambda_h}$. We also note that our result may be consistent with the one of [6]

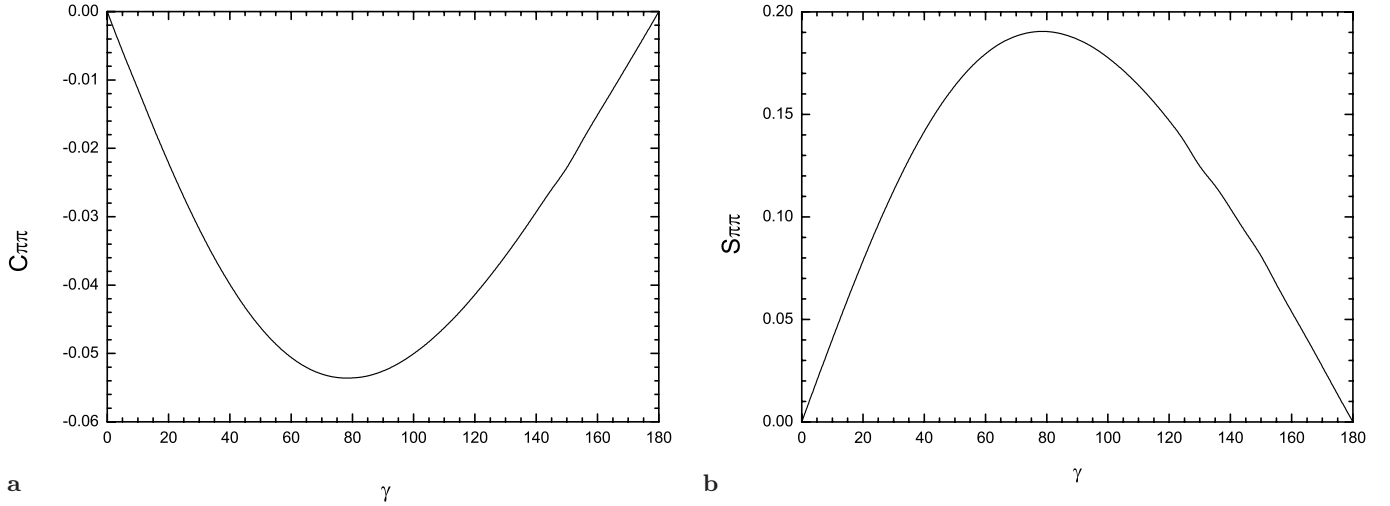


Fig. 2a,b. The direct CP violation parameter $C_{\pi\pi}$ and the mixing-induced CP violation parameter $S_{\pi\pi}$ of $\bar{B}_s \rightarrow \pi^+\pi^-$ decay as a function of the weak phase γ (in degrees)

$\text{Br}(\bar{B}_s \rightarrow \pi^+\pi^-) = (0.024_{-0.003-0.012}^{+0.003+0.025+0.163}) \times 10^{-6}$ if the huge uncertainties are considered. In a recent study in the framework of the pQCD factorization [21], the authors found $\text{Br}(\bar{B}_s \rightarrow \pi^+\pi^-) = (4.2 \pm 0.6) \times 10^{-7}$, where the endpoint divergence is regulated by k_{\perp}^2 .

The absolute ratio between the amplitude of penguin and tree is $z = 9.8$, and the strong phase is $\delta = 164^\circ$. So we can see that almost the whole contribution comes from the penguin. Our results for z and δ agree with the pQCD results [21].

Now it is time to discuss CP asymmetries of $\bar{B}_s(B_s) \rightarrow \pi^+\pi^-$. The time-dependent asymmetries are given by [22]

$$A_{CP}(t) \equiv \frac{\Gamma(\bar{B}_s(t) \rightarrow \pi^+\pi^-) - \Gamma(B_s(t) \rightarrow \pi^+\pi^-)}{\Gamma(\bar{B}_s(t) \rightarrow \pi^+\pi^-) + \Gamma(B_s(t) \rightarrow \pi^+\pi^-)} = C_{\pi\pi} \cos(\Delta mt) + S_{\pi\pi} \sin(\Delta mt), \quad (14)$$

where Δm is the mass difference of the two mass eigenstates of the B_s meson. $C_{\pi\pi}$ and $S_{\pi\pi}$ are parameters describing the direct CP violation and the mixing-induced CP violation, respectively.

Finally, our results for direct and mixing-induced CP violations in the decay are presented as functions of the weak phase γ in Fig. 2a,b respectively. For $\gamma = 60^\circ \pm 14^\circ$ [15], the direct CP violation parameter $C_{\pi\pi}$ is about -0.05 , the mixing-induced CP violation parameter $S_{\pi\pi}$ of the decay is as large as 0.18.

In summary, we have calculated the CP averaged branching ratio and the CP asymmetries of the decay $\bar{B}_s \rightarrow \pi^+\pi^-$ within the framework of QCD factorization. We have obtained that the CP averaged branching ratio of this decay mode is of the order of 10^{-7} . The CP violations are estimated to be $C_{\pi\pi} = -0.05$, $S_{\pi\pi} = 0.18$. Compared with former studies in the same framework, we have included both the two distribution functions Φ_+^B and Φ_-^B of the B_s meson. We also have used the Cornwall prescription [7] for the gluon propagator with a dynamical mass to avoid enhancements in the soft endpoint region. It is noted that recent studies [8,9] have given support for the Corn-

wall prescription, which might have many phenomenological applications in B decays. Once future measurements at LHC-b are in agreement with our predictions, it would indicate that the Cornwall prescription could be used in QCDF to improve its treatment of endpoint divergences in hard-spectator scattering and annihilation topologies to enhance its power for analyzing charmless B non-leptonic decays.

Acknowledgements. This work is supported by NFSC under contract No.10305003, Henan Provincial Foundation for Prominent Young Scientists under contract No.0312001700 and in part by the project sponsored by SRF for ROCS, SEM.

References

1. BaBar Collaboration, <http://www-public.slac.stanford.edu/babar/BaBarPublications>
2. Belle Collaboration, <http://belle.kek.jp/>
3. M. Wirbel, B. Stech, M. Bauer, Z. Phys. C **29**, 637 (1985); M. Bauer, B. Stech, M. Wirbel, Z. Phys. C **34**, 103 (1987); L. -L. Chau, H. -Y. Cheng, W.K. Sze, H. Yao, B. Tseng, Phys. Rev. D **43**, 2176 (1991); Erratum D **58**, 019902 (1998)
4. M. Beneke, G. Buchalla, M. Neubert, C.T. Sachrajda, Phys. Rev. Lett. **83**, 1914 (1999); Nucl. Phys. B **579**, 313 (2000)
5. H.n. Li, H.L. Yu, Phys. Rev. Lett. **74**, 4388 (1995); Phys. Lett. B **353**, 301 (1995); Y.Y. Keum, H.n. Li, A.I. Sanda, Phys. Rev. D **63**, 054008 (2001)
6. M. Beneke, M. Neubert, Nucl. Phys. B **675**, 333 (2003)
7. J.M. Cornwall, Phys. Rev. D **26**, 1453 (1982); J.M. Cornwall, J. Papavasiliou, Phys. Rev. D **40**, 3474 (1989); D **44**, 1285 (1991)
8. L. von Smekal, R. Alkofer, A. Hauck, Phys. Rev. Lett. **79**, 3591 (1997), hep-ph/9705242; D. Zwanziger, Phys. Rev. D **69**, 016002 (2004), hep-ph/0303028; D.M. Howe, C.J. Maxwell, Phys. Lett. B **541**, 129 (2002), hep-ph/0204036; Phys. Rev. D **70**, 014002 (2004), hep-ph/0303163; A.C. Aguilar, A.A. Natale, P.S. Rodrigues da Silva, Phys. Rev. Lett. **90**, 152001 (2003), hep-ph/0212105;

- S. Furui, H. Nakajima, hep-lat/0309166, AIP Conf. Proc. **717**, 685 (2004)
9. S. Brodsky, S. Menke, C. Merino, J. Rathsman, Phys. Rev. D **67**, 055008 (2003), hep-ph/0212078; A.C. Mattingly, P.M. Stevenson, Phys. Rev. D **49**, 437 (1994), hep-ph/9307266; M. Baldicchi, G.M. Prosperi, Phys. Rev. D **66**, 074008 (2002)
10. G. Buchalla, A.J. Buras, M.E. Lautenbacher, Rev. Mod. Phys. **68**, 1125 (1996)
11. A.G. Grozin, M. Neubert, Phys. Rev. D **55**, 272 (1997); M. Beneke, F. Feldmann, Nucl. Phys. B **592**, 3 (2001)
12. S. Descotes-Genon, C.T. Sachrajda, Nucl. Phys. B **625**, 239 (2002)
13. P. Ball, V.M. Braun, Phys. Rev. D **58**, 094016 (1998); P. Ball, JHEP **9901**, 010 (1999)
14. T. Huang, X.G. Wu, Phys. Rev. D **70**, 093013 (2004), hep-ph/0408252
15. S. Eidelman et al., Phys. Lett. B **592**, 1 (2004)
16. M. Beneke et al., Nucl. Phys. B **606**, 245 (2001); S.W. Bosch, G. Buchalla, Nucl. Phys. B **621**, 459 (2002); M. Beneke, T. Feldmann, D. Seidel, Nucl. Phys. B **612**, 25 (2001)
17. M. Beneke, M. Neubert, Nucl. Phys. B **675**, 333 (2003)
18. J.F. Sun, G.H. Zhu, D.S. Du, Phys. Rev. D **68**, 054003 (2003)
19. A.G. Williams et al., hep-ph/0107029 and references therein
20. R. Alkofer, L. von Smekal, Phys. Rept. **353**, 281 (2001), and references therein
21. Y. Li, C.D. Lü, Z.J. Xiao, X.Q. Yu, Phys. Rev. D **70**, 034009 (2004), hep-ph/0404028
22. M. Gronau, Phys. Rev. Lett. **63**, 1451 (1989)